

Modeling, Simulation and Verification of Contactless Power Transfer Systems

COMSOL Conference, Munich, 2016.

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Components and operating principle

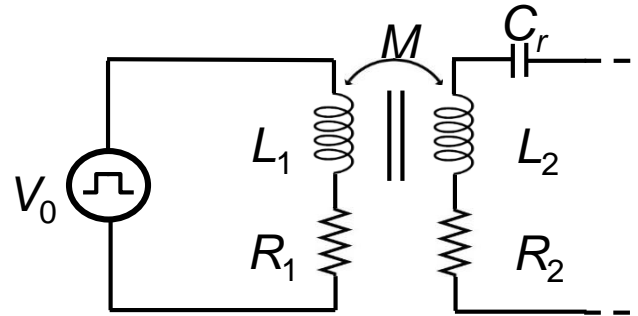
- Primary coil
- Secondary coil
- Flux concentrators
- Lenz-Faraday
- Inductive coupling



Basic schematic

- Inverter \rightarrow AC voltage \rightarrow AC current
- Loosely coupled transformer
- Receiver circuit (resonance capacitor, rectifier and load)

L : Coil inductance
 R : Coil resistance
 M : Mutual inductance
 C_r : Resonant capacitor



Definitions

- Induction efficiency:

$$\eta = \frac{\text{Transmitted power}}{\text{Total power}}$$

- Quality factor:

$$Q_1 = \frac{\omega_0 L_1}{R_1}, \quad Q_2 = \frac{\omega_0 L_2}{R_2}, \quad Q = \sqrt{Q_1 Q_2}$$

- Coupling factor:

$$k = \frac{M}{\sqrt{L_1 L_2}}$$

- Maximum efficiency [1]:

$$\eta_{max} = \frac{1}{1 + \frac{2}{(kQ)^2} \left(1 + \sqrt{1 + (kQ)^2}\right)}$$

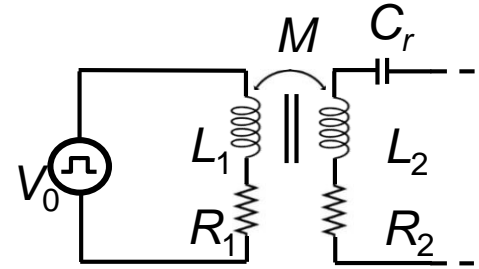
Figures of Merit

- $kQ \uparrow \iff \eta_{\max} \uparrow$

- $$kQ = \frac{M}{\sqrt{L_1 L_2}} \sqrt{\frac{(\omega_0 L_1)(\omega_0 L_2)}{R_1 R_2}}$$

- Objective:

Accurately predict the values of R_1 , R_2 , L_1 , L_2 and M .

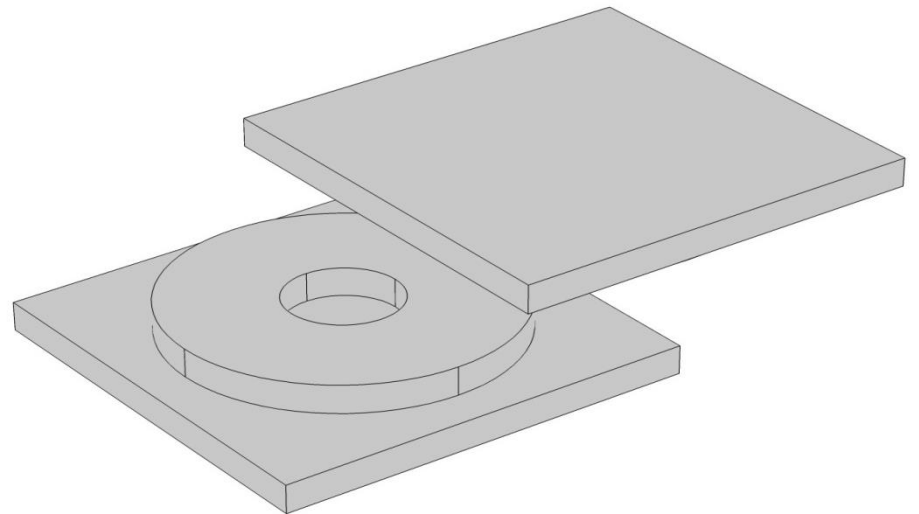


Simulation in COMSOL

- AC/DC module - Magnetic Fields
- Frequency domain
- 2D Axisymmetric simulation if coils are aligned (same revolution axis)
- 3D simulation if coils are misaligned (different revolution axes)

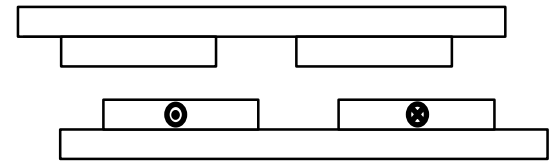
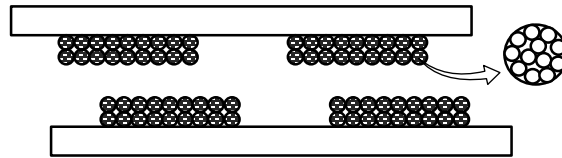
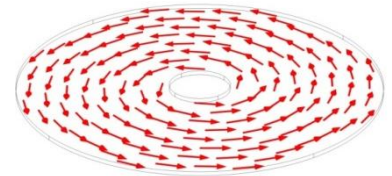
Geometry and materials

- Ring-type inductors.
 - Ideal non-lossy material ($\sigma \approx 0 \text{ S/m}$, $\mu = 1$)
- Ferrite blocks
 - $\sigma \approx 0 \text{ S/m}$, $\mu = 2000$



Physics – AC/DC Magnetic Fields

- Primary coil: External current density
 - Assuming multi-stranded Litz wire the current across the inductor's cross-section can be assumed constant.



Induced voltage calculation

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- $V(\omega) = -\oint \vec{\mathbf{E}}(\omega) \cdot d\vec{\mathbf{l}} = -\frac{1}{S_{\text{turn}}} \int_{V_{\text{coil}}} E_{\varphi}(\omega) dV$
- Advisable to work in 2 physics:
- mf1
 - Set 1 A in coil 1
 - Obtain V in both coils
- mf2
 - Set 1 A in coil 2
 - Obtain V in both coils

Inductance calculation

- $Z(\omega) = \frac{V(\omega)}{I(\omega)}$

- $L(\omega) = \frac{\Im(Z(\omega))}{\omega}$

- mf1

$$L_1(\omega) = \frac{\Im(V_1(\omega) / I_1(\omega))}{\omega}$$

$$M(\omega) = \frac{\Im(V_2(\omega) / I_1(\omega))}{\omega}$$

- mf2

$$L_2(\omega) = \frac{\Im(V_2(\omega) / I_2(\omega))}{\omega}$$

$$M(\omega) = \frac{\Im(V_1(\omega) / I_2(\omega))}{\omega}$$



Resistance calculation

- Resistance of Litz wire: $R_w = R_{\text{cond}} + R_{\text{prox}}$

- Dc and skin effect losses: R_{cond}

- Caused by the current driven when applying an external voltage

- Proximity effect: R_{prox}

- Caused by the current induced by neighboring conductors

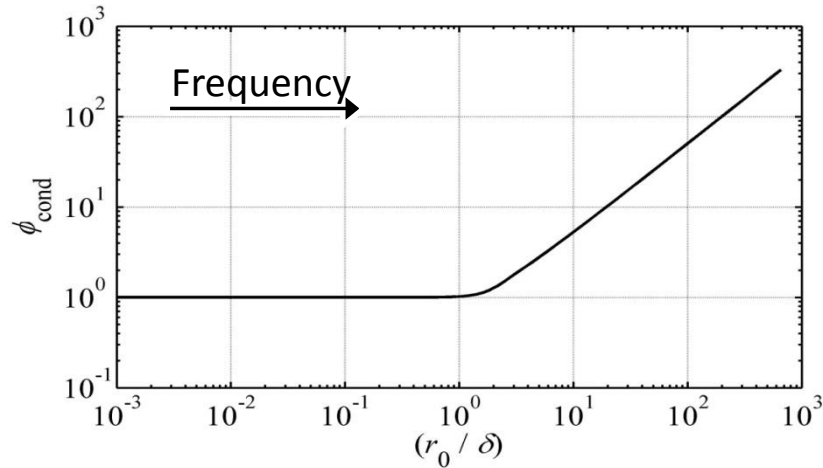


Resistance calculation

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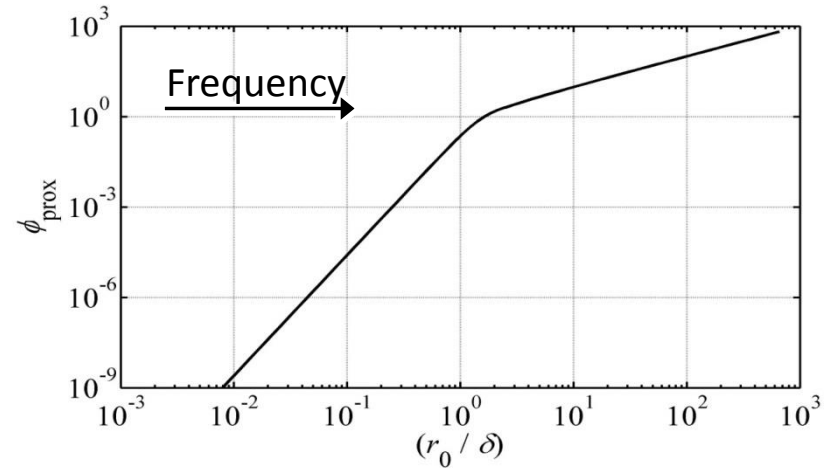
- $$R_{cond} = \frac{nl_{avg}}{n_s \pi r_0^2 \sigma} \Phi_{cond} (r_0 / \delta)$$

[2]



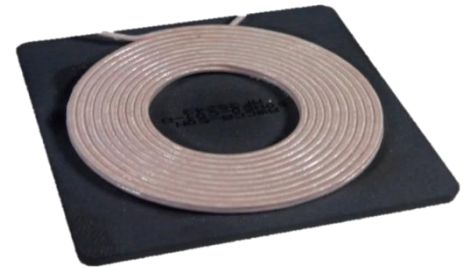
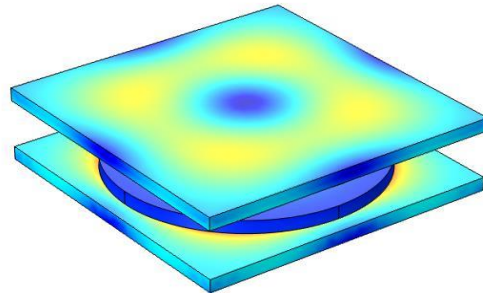
- $$R_{prox} = \frac{n^3 n_s 4\pi}{\sigma} \Phi_{prox} (r_0 / \delta) \left\langle |\bar{H}_t|^2 \right\rangle_{coil}$$

[2]

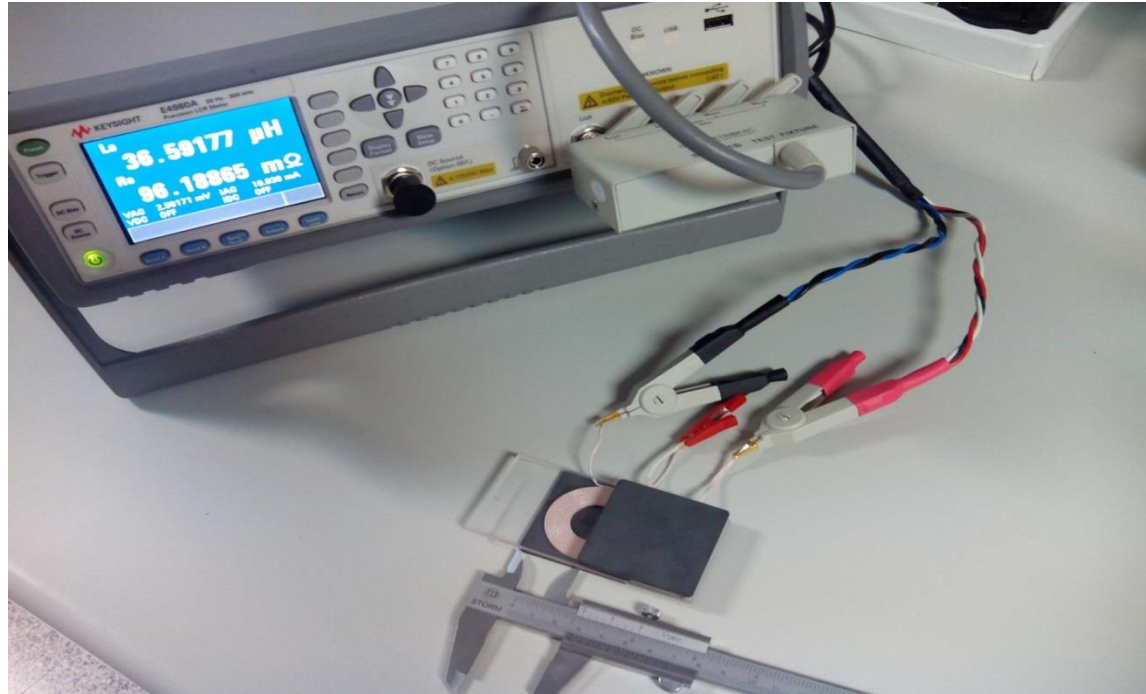


Experimental verification

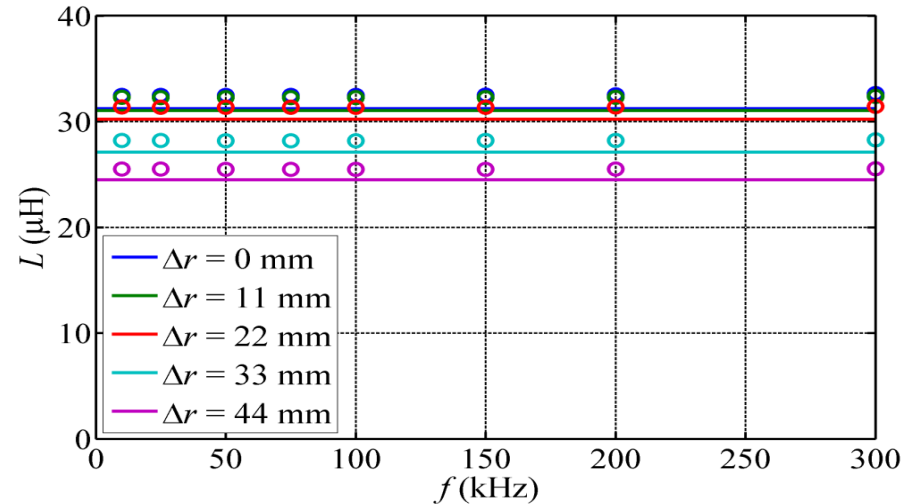
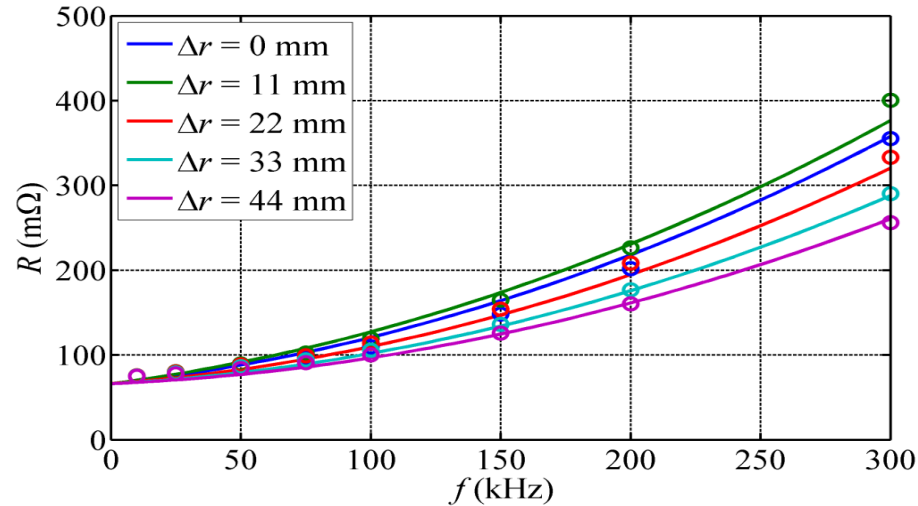
- 2 identical coils: $R_1 = R_2$ and $L_1 = L_2$
- 20 turns of 105 strands (\varnothing 80 μ m)
- Ext. radius: 22 mm - Int. radius: 10.12 mm.
- Coil separation: 4 mm.



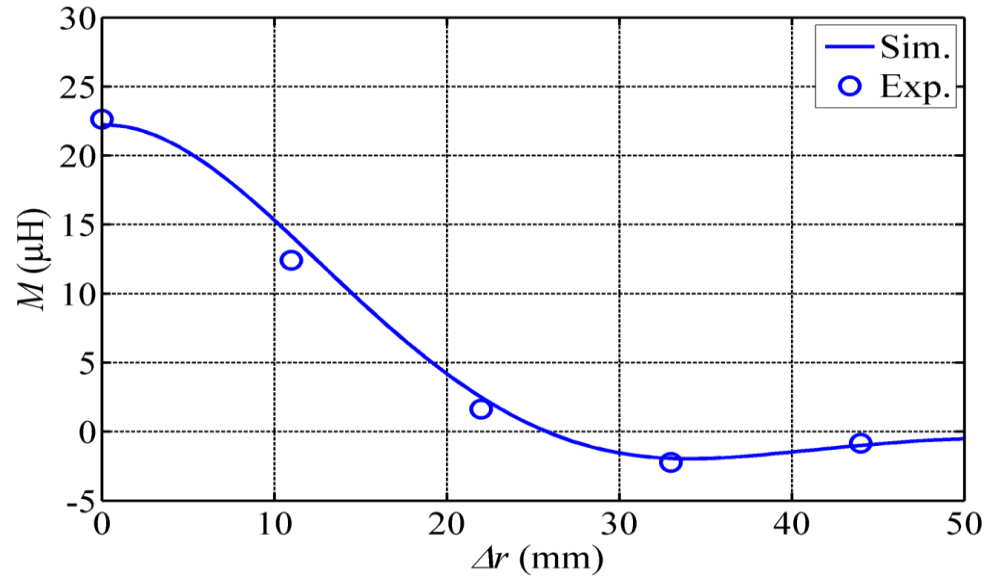
Experimental verification



Experimental verification



Experimental verification



Conclusions

- Accurate results with low computational cost (cabling structure is not simulated).
- Flexible and versatile:
 - Multi-coil WPT systems
 - Different cabling structures
 - solid wire, litz wire, PCB tracks...
 - Induction heating

Thanks for your attention!



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