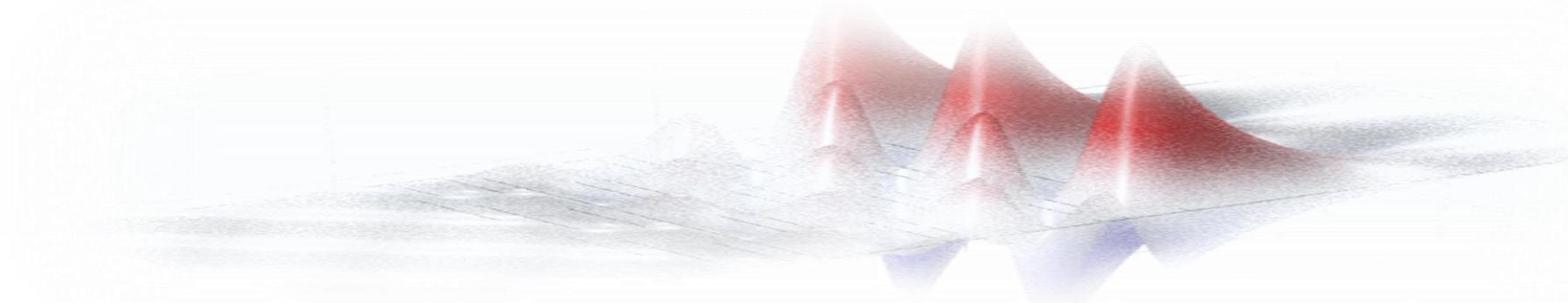


# Highly Sensitive Grating-coupled Bloch Surface Wave Resonance Bio-sensor via Azimuthal Interrogation

Vijay Koju, William M. Robertson  
Middle Tennessee State University  
6 October 2016

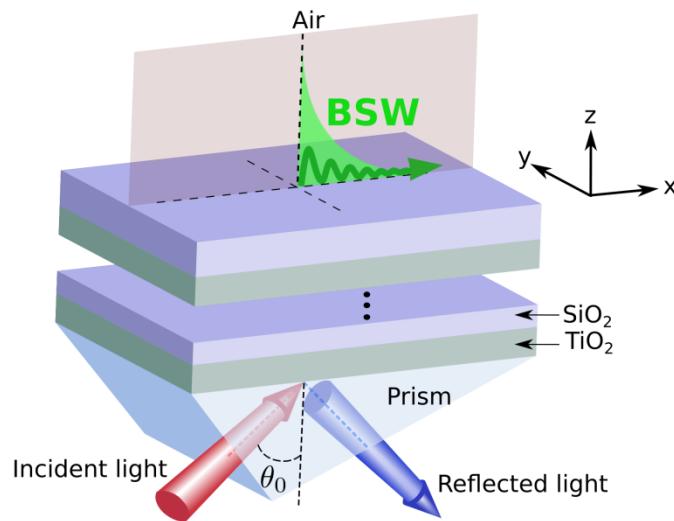


# Bloch Surface Wave (BSW)

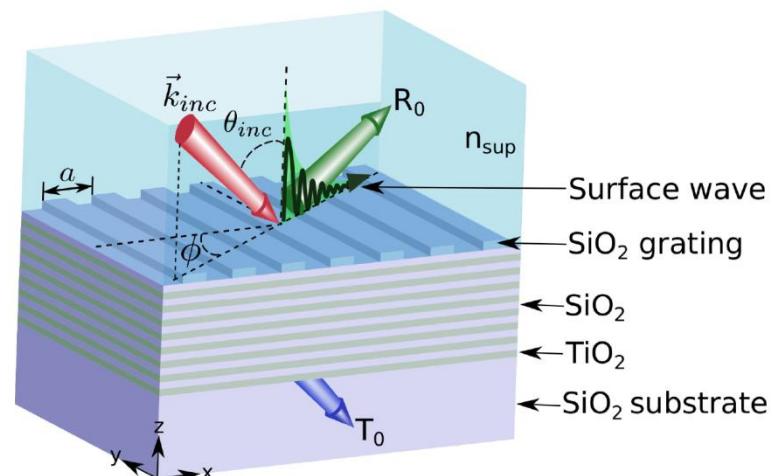
- Electromagnetic excitations that propagate at the interface between a dielectric-dielectric interface
- Evanescently confined in the perpendicular direction to the propagation
- Enhanced electric field intensity at the confinement
- Applications in label-free and fluorescence bio-sensing

# BSW excitation

Prism coupling



Grating coupling



# Physics

- Maxwell's Wave Equation: 
$$\nabla \times \mu_r^{-1}(\nabla \times \vec{E}) - k_0^2 \left( \epsilon_r - \frac{j\sigma}{\omega \epsilon_0} \right) \vec{E} = \vec{0}$$
For:  $\mu_r = 1$ ,  $\epsilon_r = n^2$ ,  $\sigma = 0$
- Reduced Maxwell's Equation: 
$$\nabla \times (\nabla \times \vec{E}) - k_0^2 n^2 \vec{E} = \vec{0}$$
- *Electromagnetic Waves, Frequency Domain (emw)* physics interface is used to solve governing equation

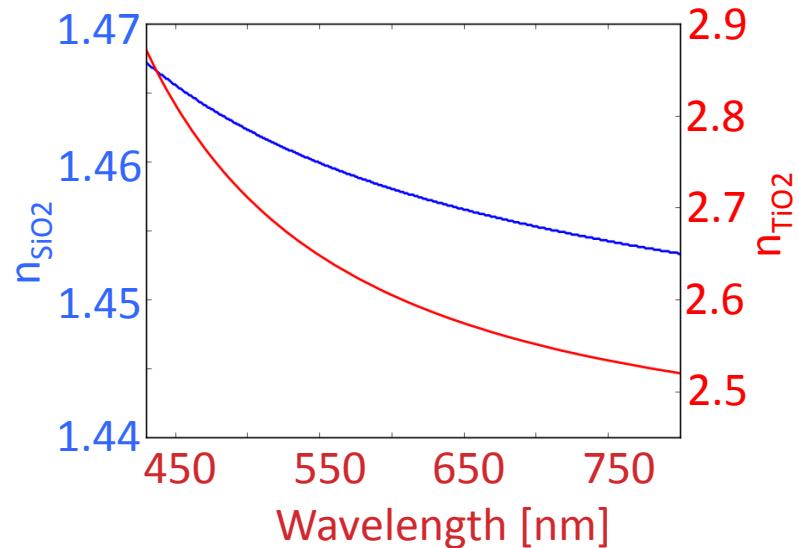
# Materials Properties

- Titanium Dioxide ( $\text{TiO}_2$ )

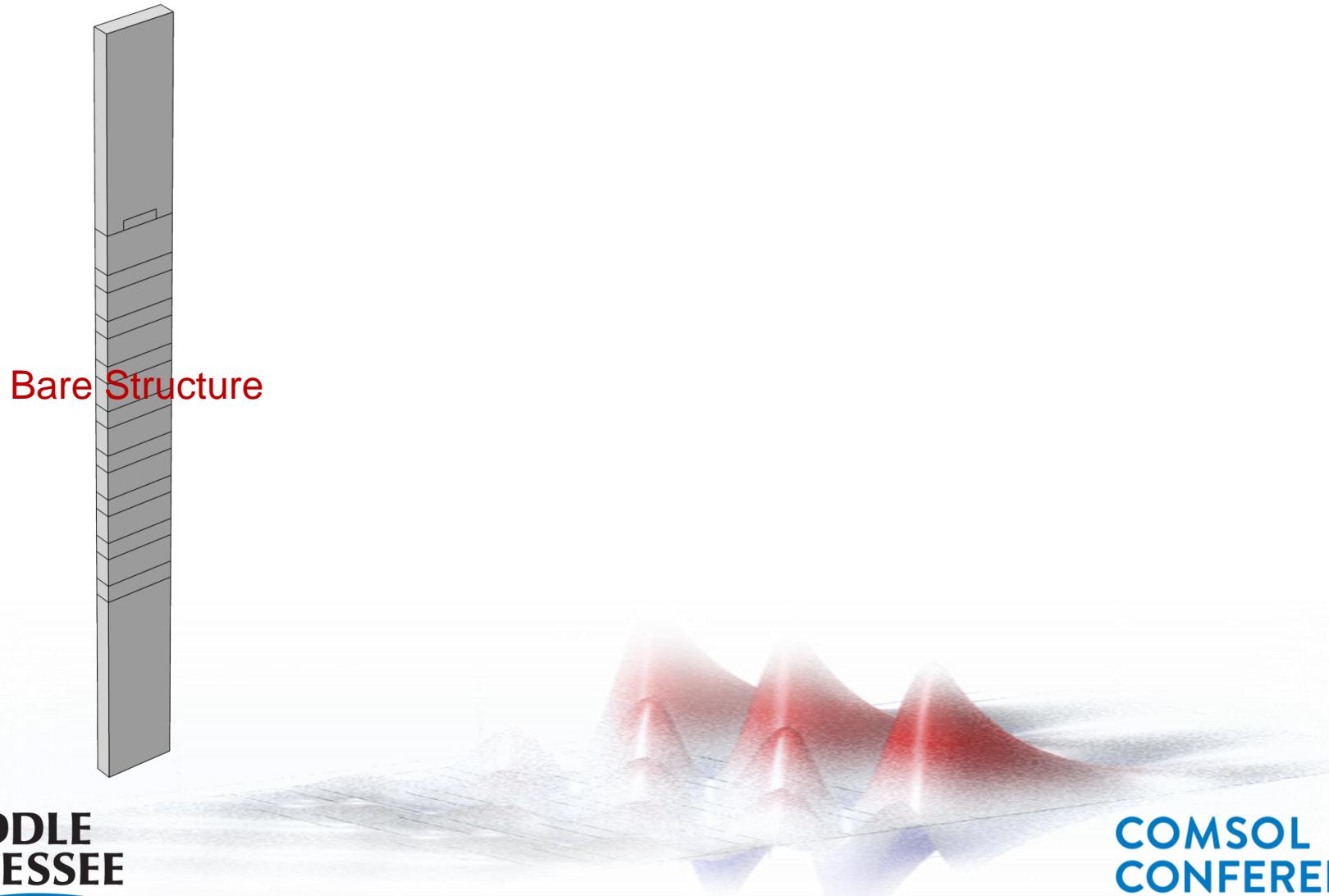
$$n_{\text{TiO}_2} = \left( 5.913 + \frac{0.2441}{\lambda^2 - 0.0803} \right)^{\frac{1}{2}}$$

- Silicon Dioxide ( $\text{SiO}_2$ )

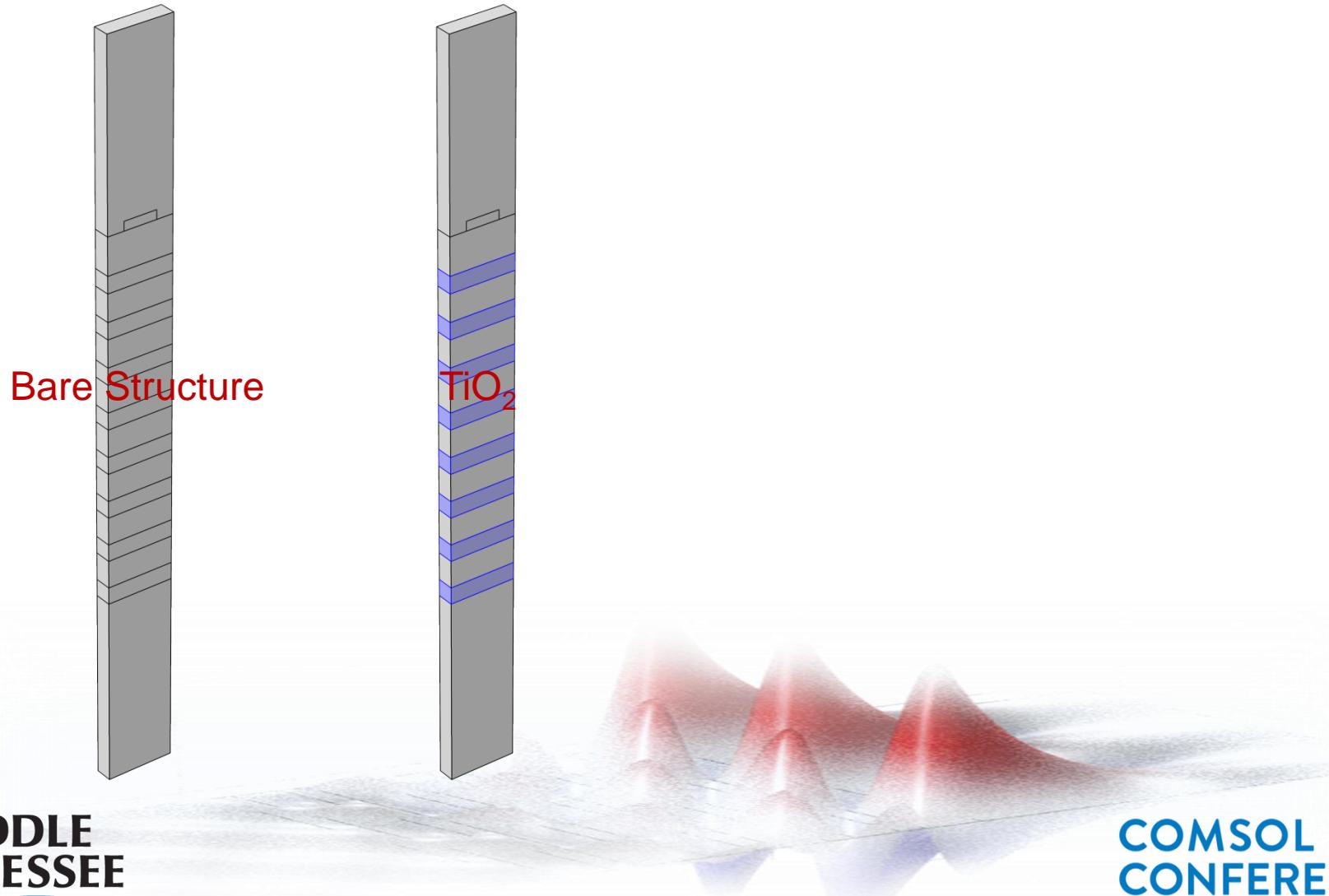
$$n_{\text{SiO}_2} = \left( 1 + \frac{0.6962\lambda^2}{\lambda^2 - 0.0684^2} + \frac{0.4079\lambda^2}{\lambda^2 - 0.1162^2} + \frac{0.8975\lambda^2}{\lambda^2 - 9.8961^2} \right)^{\frac{1}{2}}$$



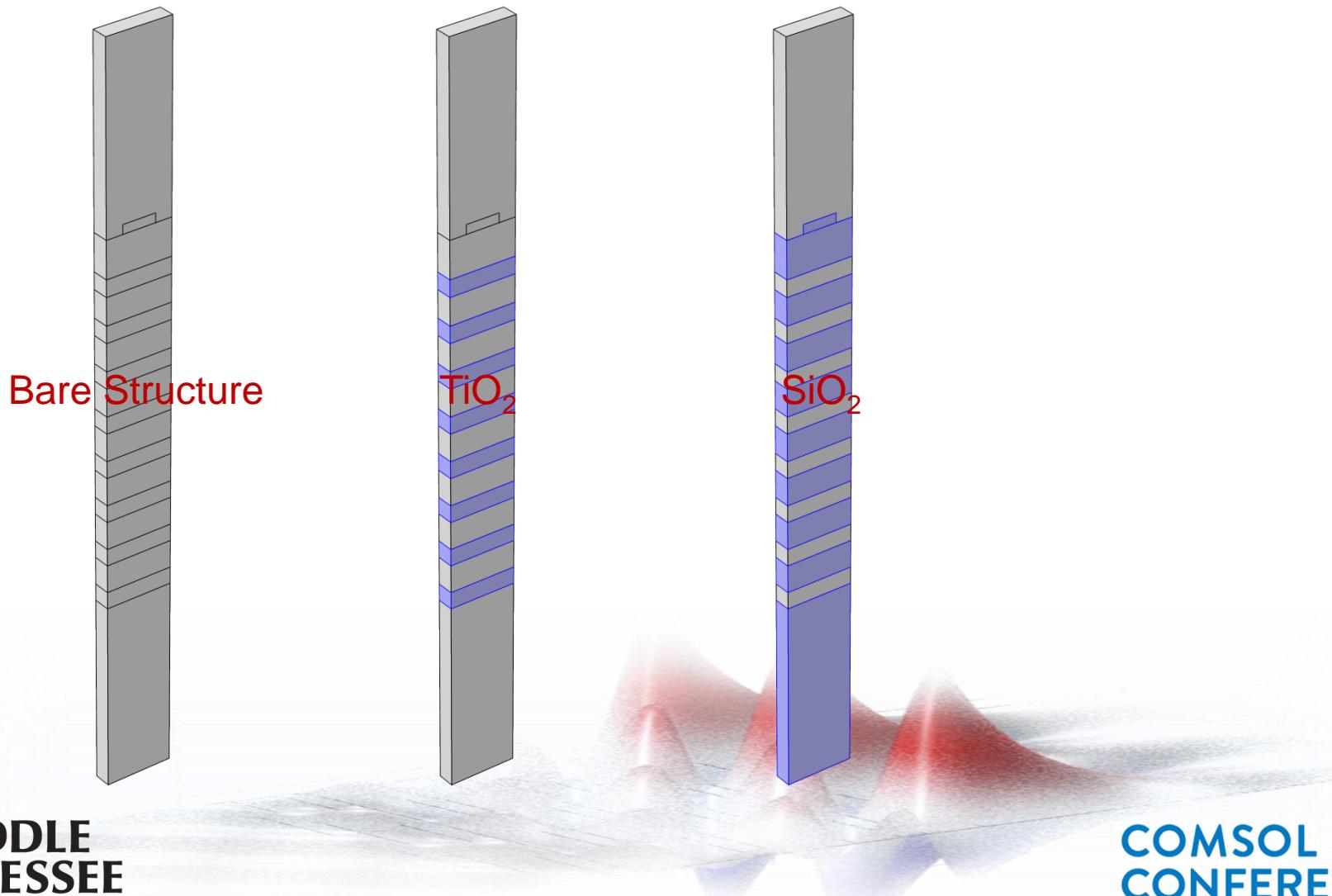
# COMSOL Model



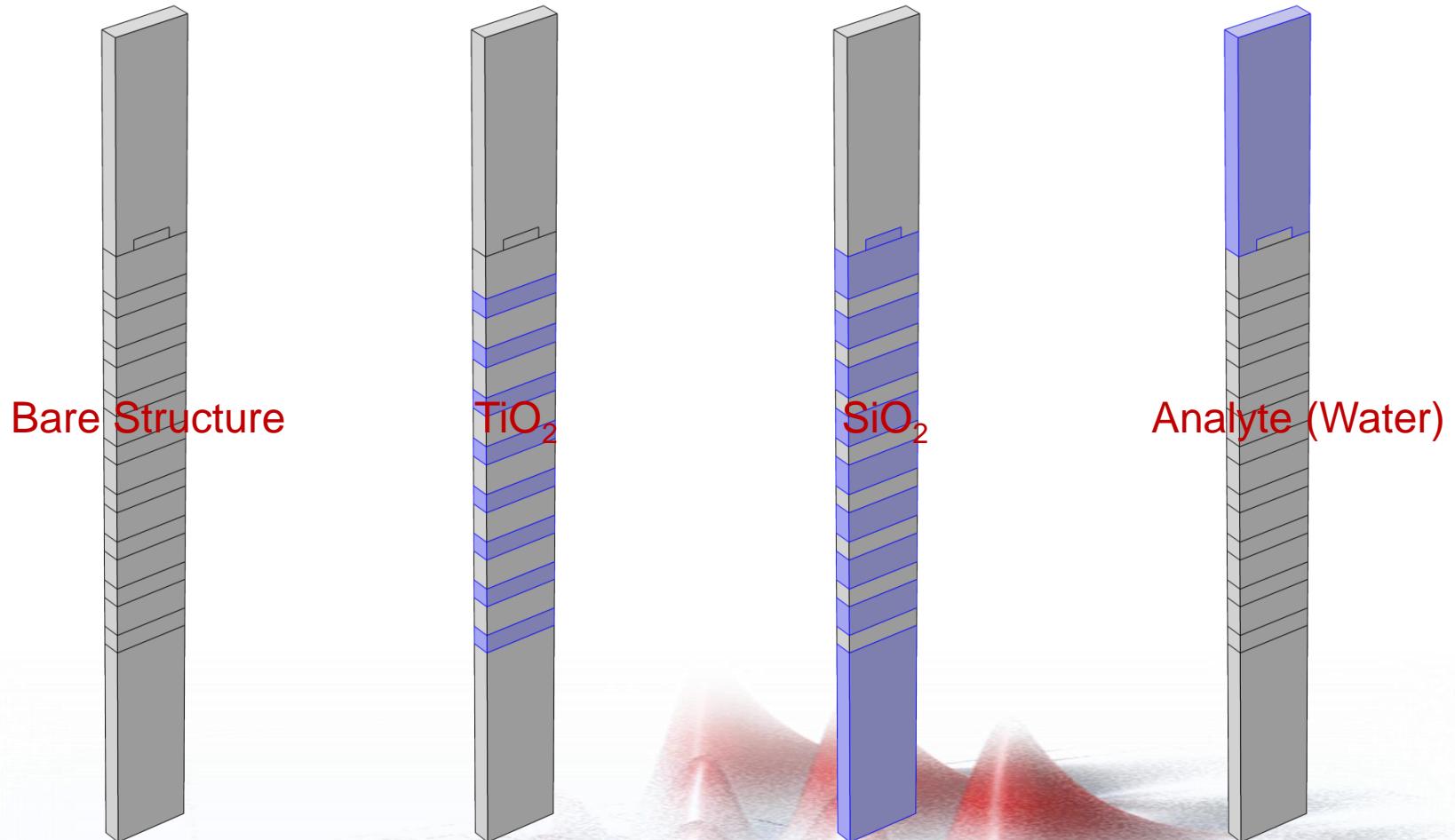
# COMSOL Model



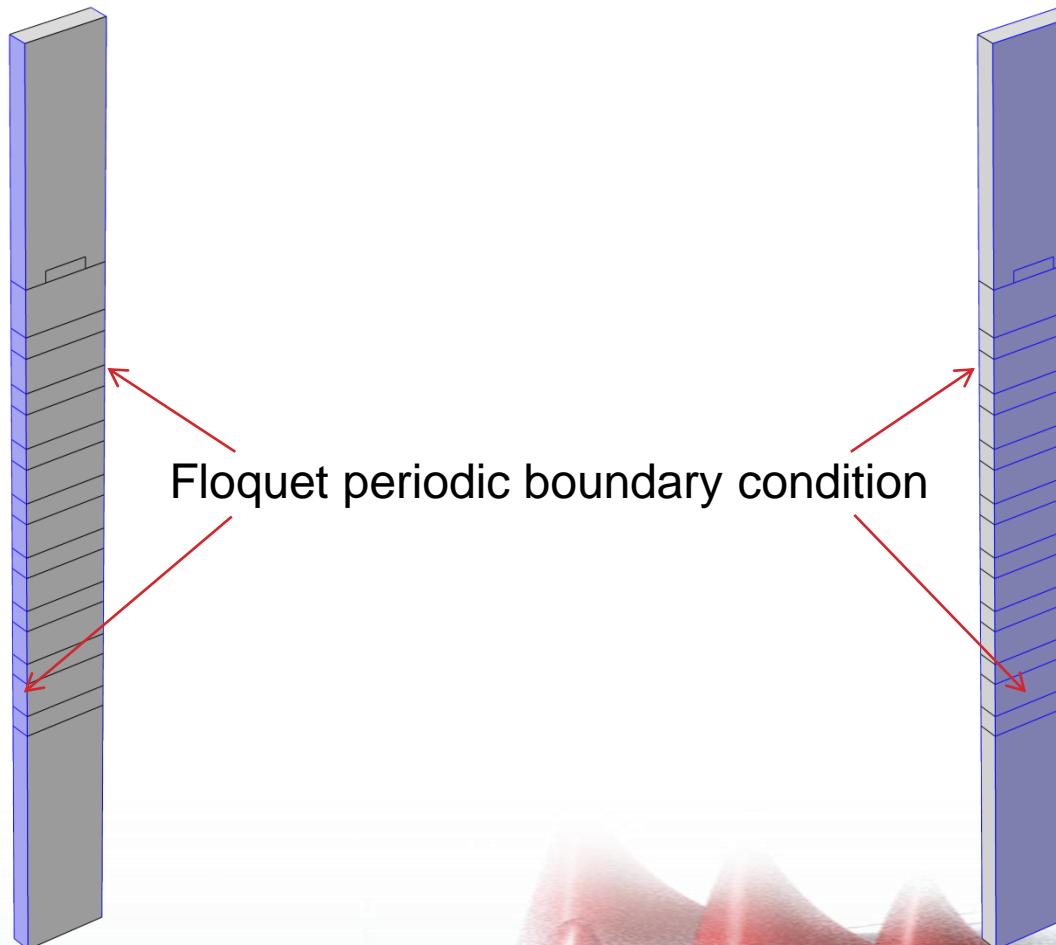
# COMSOL Model



# COMSOL Model



# Boundary Conditions



# Boundary Conditions



Input Port

## Input Port parameters

### Port Mode Settings

Input quantity:

Electric field

Electric mode field amplitude:

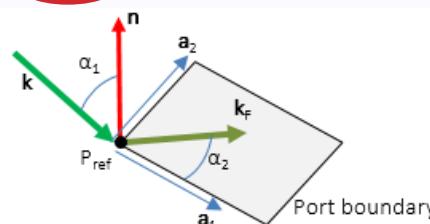
E <sub>0</sub>	sin(phi)	x	V/m
	cos(phi)	y	
	0	z	

Elevation angle of incidence:

$\alpha_1$  theta rad

Azimuth angle of incidence:

$\alpha_2$  phi rad



Output Port

## Output Port parameters

### Port Mode Settings

Input quantity:

Electric field

Electric mode field amplitude:

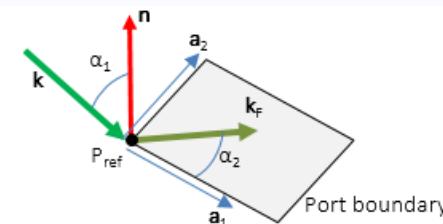
E <sub>0</sub>	sin(phi)	x	V/m
	cos(phi)	y	
	0	z	

Elevation angle of incidence:

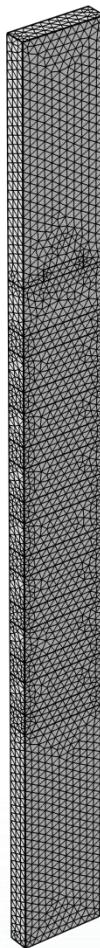
$\alpha_1$  -thetab rad

Azimuth angle of incidence:

$\alpha_2$  -phi+pi/2 rad



# Finite Element Mesh



▼ Element Size Parameters

Maximum element size:  
 m

Minimum element size:  
 m

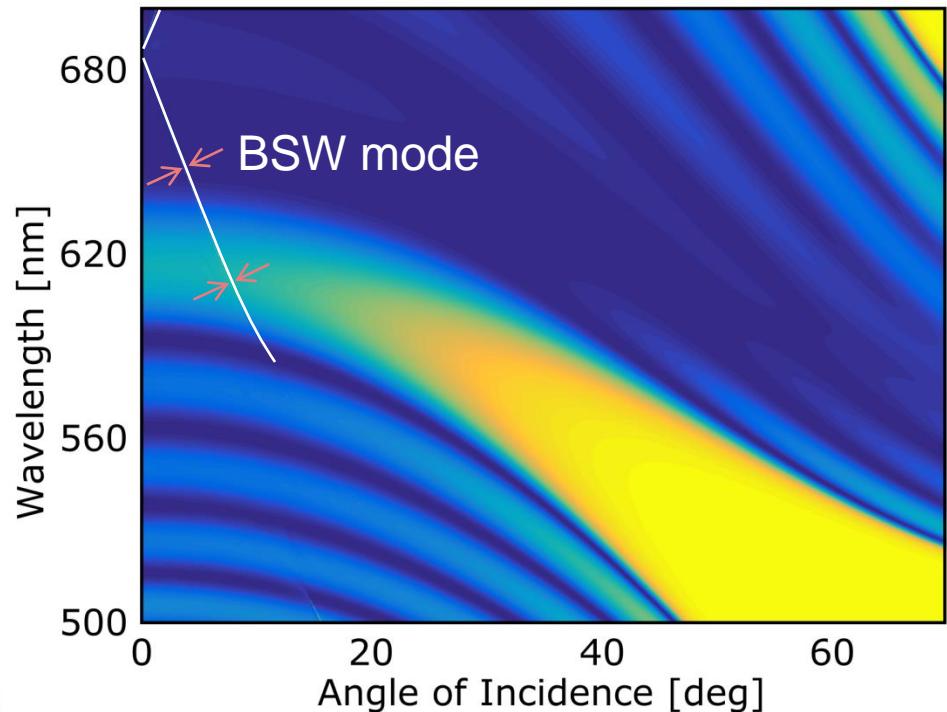
Maximum element growth rate:

Curvature factor:

Resolution of narrow regions:

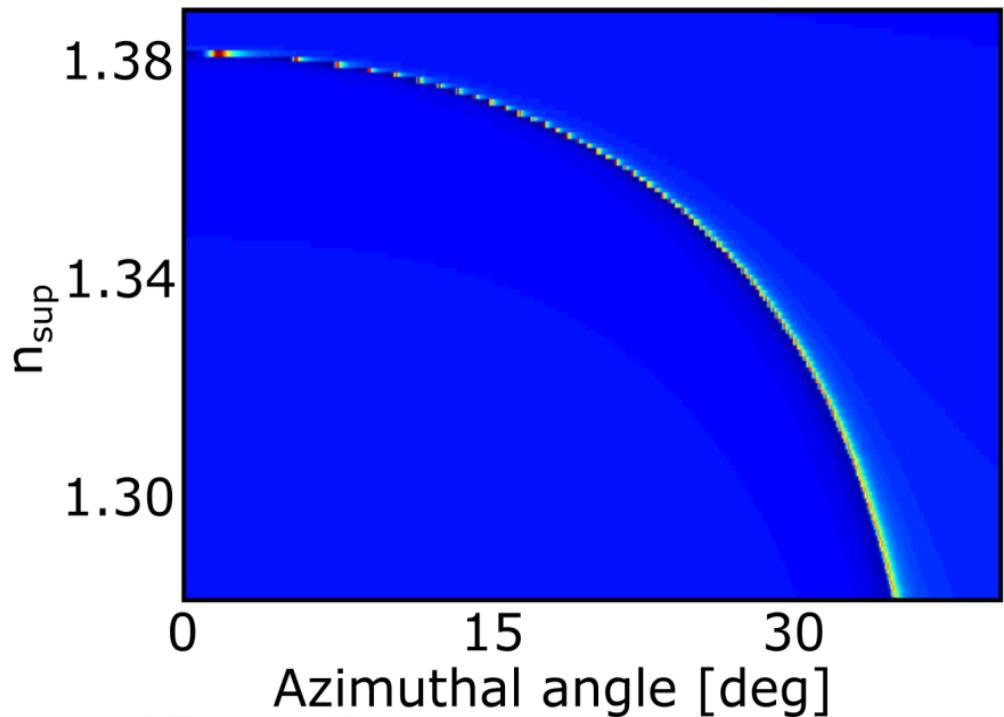
# Reflectivity Map

- Azimuthal angle  $\varphi = 0$
- Superstrate/Analyte refractive index  $n_{sup} = 1.33$

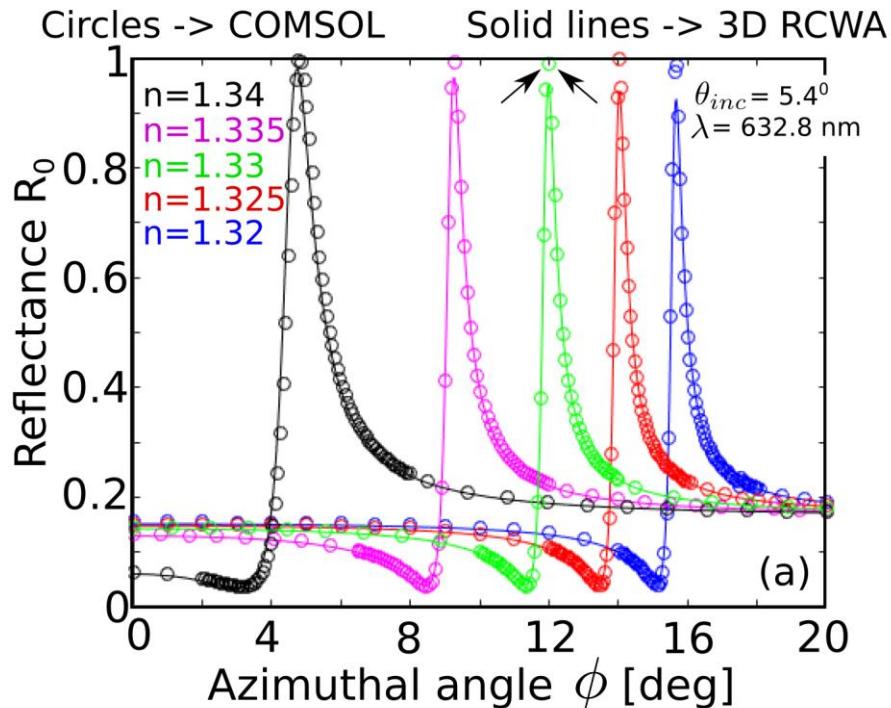


# Azimuthal Sensitivity

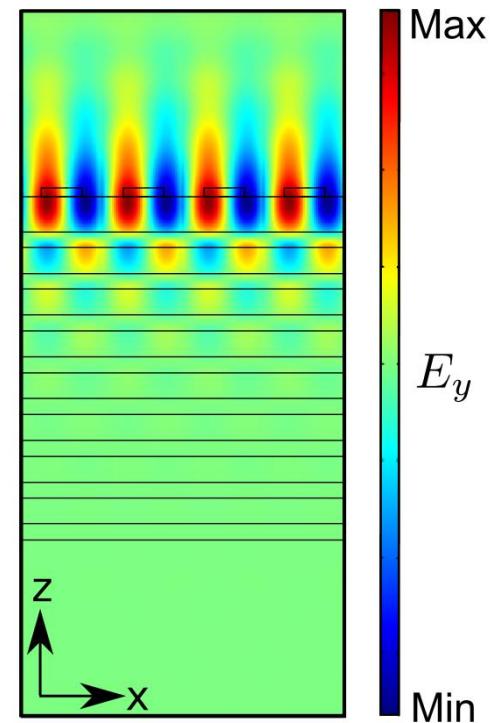
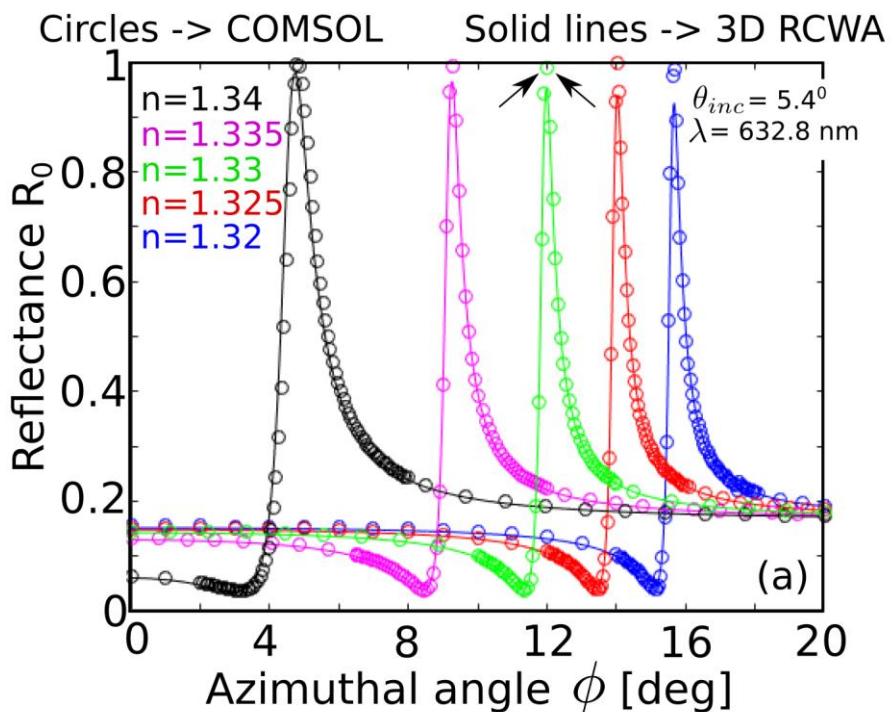
- Wavelength  $\lambda = 632.8 \text{ nm}$
- Incident angle  $\theta_{inc} = 5.8^\circ$
- $S_{n_{sup}} = \frac{\Delta\varphi}{\Delta n_{sup}}$
- $S_{n_{sup}} \sim 1200^\circ/\text{RIU}$



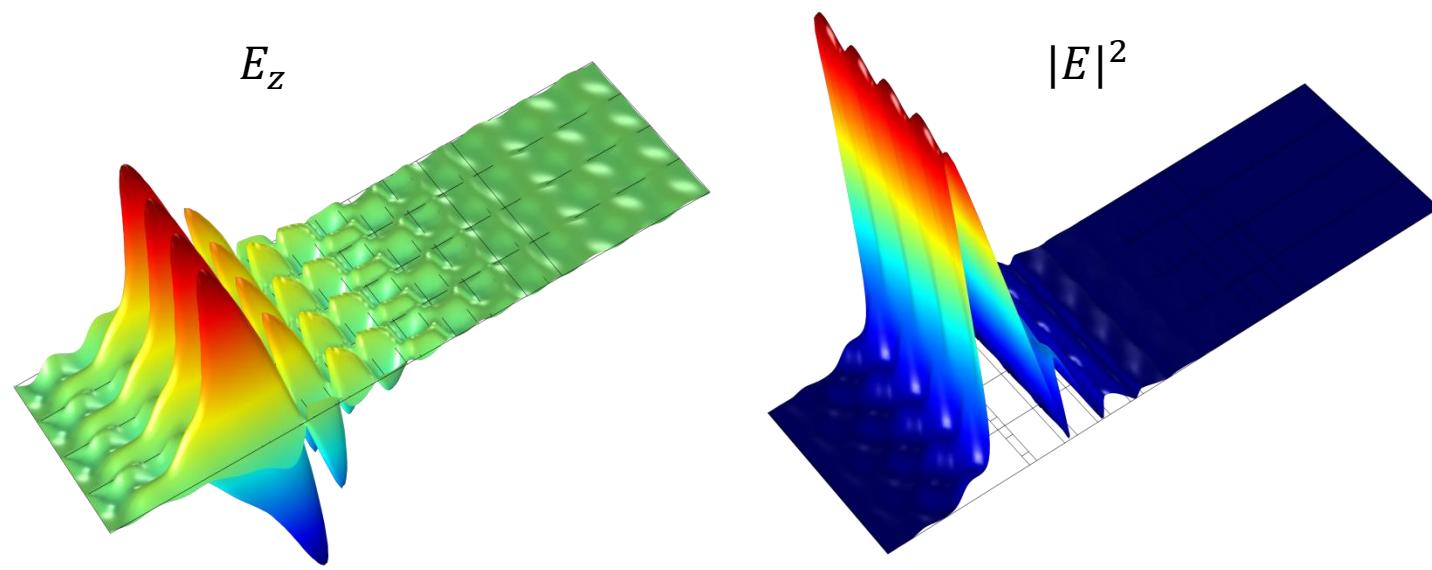
# Azimuthal Sensitivity



# Azimuthal Sensitivity



# E-Field Profile at BSW Resonance



# Summary

- Grating-coupled BSW resonance sensor
- Azimuthal interrogation
- Enhanced refractive index sensitivity