Study on Borehole Stability of Shale Gas Well under Multi-field Coupling

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Introduction

The mechanical response of mud shale under the action of multiple field coupling is always a hot topic in the field of drilling engineering. In this paper, a multi-field coupled model is established, using the solid mechanics module embedded in COMSOL and combined with the General form in PDE module to complete the setting of the model. The grid encryption function is used to encrypt the area around the well, which makes the calculation results more advanced and more in line with the actual situation on site. The results show that the collapse process of rock around the shaft wall is a dynamic evolution process involving space and time, and COMSOL can well simulate the above 4-D process. The simulation results can be used to analyze and simulate the effect of time dependence on wellbore stability during drilling. It can also help drilling engineers design drilling plans (including design and calculation of mud safety density window, mud salinity, etc.).

Coupling model

Navier equations for displacements: A momentum balance equation is employed to derive the Naviertype equation for displacements as:

$$(K + \frac{G}{3})\nabla(\nabla u) + G\nabla^2 u - \alpha \nabla p + \omega_0 \chi a \nabla C^S - \gamma_1 \nabla T = 0$$
(1)

where K and G are bulk and shear moduli, u is the rock displacement and T is the temperature of the porous medium.

Pressure diffusion equation: Using conservation of mass for a weakly compressible fluid along with the expression for the flux gives a coupled fluid diffusion equation as:

$$\frac{\alpha \partial \varepsilon_{ii}}{\partial t} + (Q + B) \frac{\partial p}{\partial t} + \beta \chi \frac{\partial C^{S}}{\partial t} - \gamma_{2} \frac{\partial T}{\partial t} = \frac{k}{u} \nabla^{2} p - \frac{k \Re \rho_{f} aRT}{u c M^{S}} \nabla^{2} C^{S} - K^{T} \nabla T$$
(2)

where α is the Biot's Coefficient, p is pore pressure, k is permeability, the fluid viscosity is μ . \mathcal{E}_{ii} and C^S are the components of total strain tensors and solute mass fractions. Also, \mathfrak{R} is the standard solute reflection coefficient (or membrane efficiency), R is the universal gas constant. M^S is the molar mass of the solute. K^T is the thermal osmosis coefficient.

Equation for solute diffusion: Conservation of a solute mass in rock yields the following equation for solute transfer:

$$\phi \frac{\partial C^{S}}{\partial t} - D\nabla^{2}C^{S} - C^{S}D^{T}\nabla^{2}T = 0$$
(3)

Where D is the solute diffusion coefficient and K^{T} is the coefficient of thermal diffusion.

Equation for thermal conduction: Conservation of energy balance in the rock yields the following equation for thermal conduction:

$$\frac{\partial T}{\partial t} - c^T \nabla^2 T = 0 \tag{4}$$

Where c^T is thermal diffusivity.

The coefficients in the governing equations are:

$$\chi = (1 - \frac{C_{mean}^{S}}{cRT\rho_{f}}) \qquad c = C_{mean}^{D} \qquad a = \frac{1}{C_{mean}^{S}} \qquad \alpha' = (\alpha - \frac{M^{S}\omega_{0}}{cRT\rho_{f}})$$

$$B' = \frac{\omega_{0}(\alpha - 1)}{K} \frac{M^{S}}{cRT\rho_{f}} \qquad Q' = (Q + \frac{\phi}{K_{f}}) \qquad Q = \frac{(\alpha - \phi)}{K_{S}}$$

$$\gamma_{1} = K\alpha_{m} + \frac{s_{0}\omega_{0}M^{S}}{RTC_{mean}^{D}} \qquad \gamma_{2} = \alpha\alpha_{m} + (\alpha_{f} - \alpha_{m})\phi + \frac{s_{0}\omega_{0}(\alpha - 1)M^{S}}{KRTC_{mean}^{D}}$$

boundary conditions

It is assumed that compressive stress is positive and tensile stress is negative. The rock is considered as a homogenous porous medium. The plane strain hypothesis and instantaneous drilling are used to solve the non-linear system of equations. Solving the non-linear system of equations requires knowledge of the initial solute concentration, temperature and pore pressure within the flow domain:

$$C^{S}(x, y, t) = C^{S}_{Mean}(x, y)$$
 for t=0
$$P(x, y, t) = P_{i}(x, y)$$
 for t=0
$$T(x, y, t) = T_{i}(x, y)$$
 for t=0

Dirichlet type boundary condition is applied to the inner boundary for the solute concentration, temperature and pore pressure as follows:

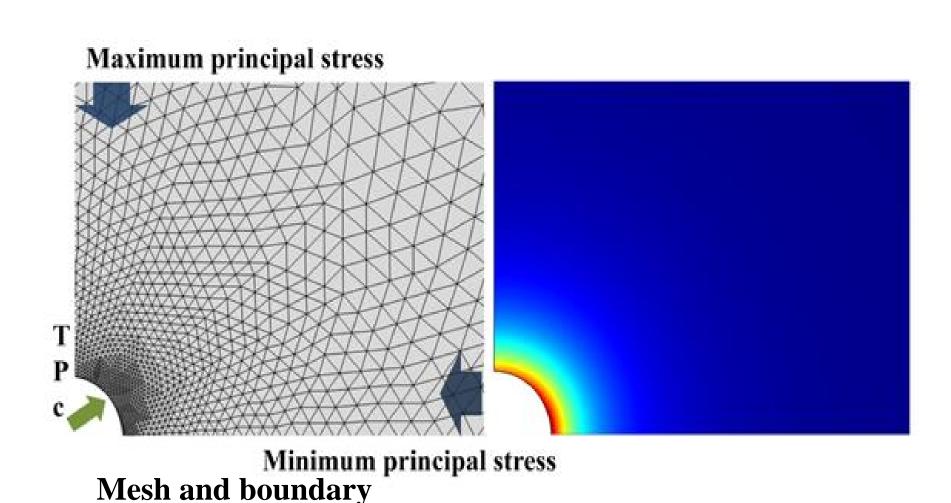
 $C^{S}(x, y, t) = C_{1}^{S}(x, y, t)$ on boundary

 $P(x, y, t) = P_1(x, y, t)$ on boundary

 $T(x, y, t) = T_1(x, y, t)$ on boundary

Calculation results

condition loading



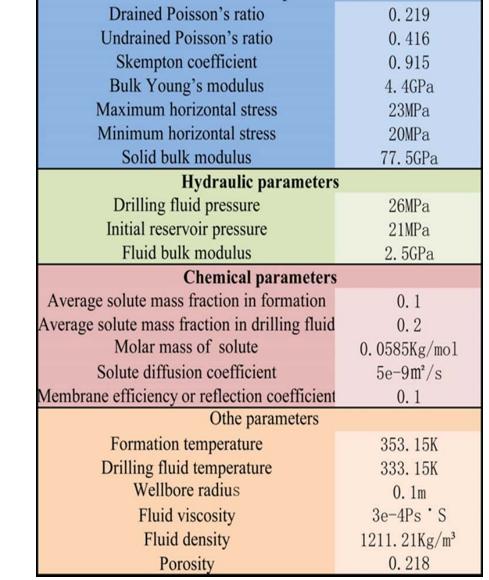


 Table 1. Basic Parameters

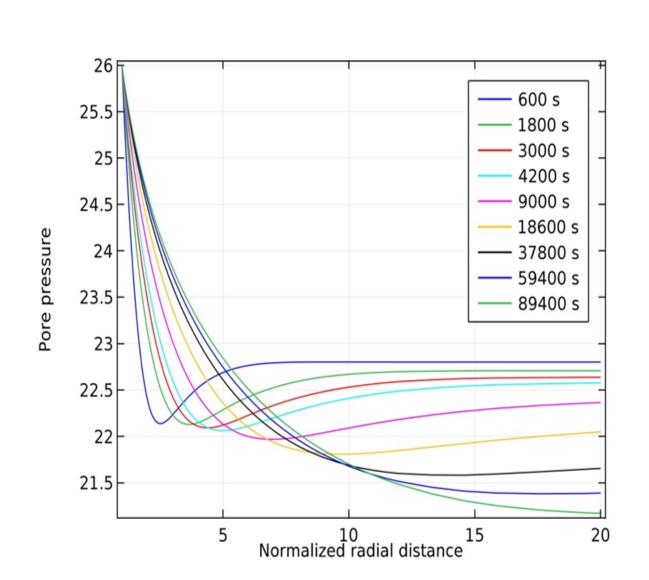
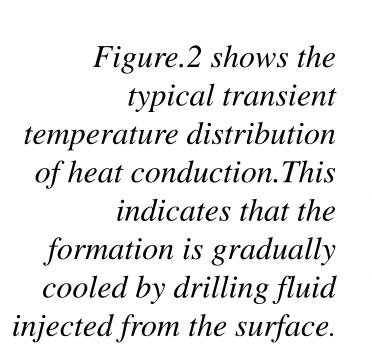
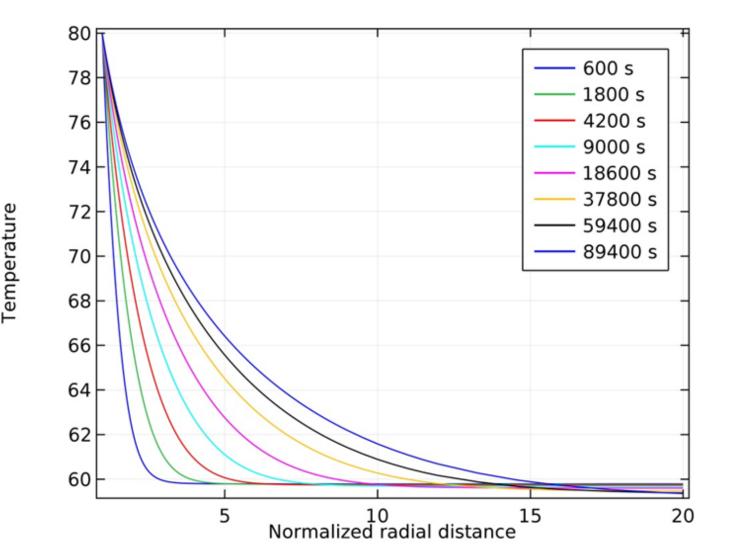


Figure.1 shows the pressure distribution near the well with time.Is the classical pressure wave transfer curve. With the time of drilling and opening the hole, the pressure wave front gradually moves along the hole radial direction from the hole wall. Meanwhile, as can be seen from the figure, its size gradually decreases. This phenomenon is caused by energy dissipation.





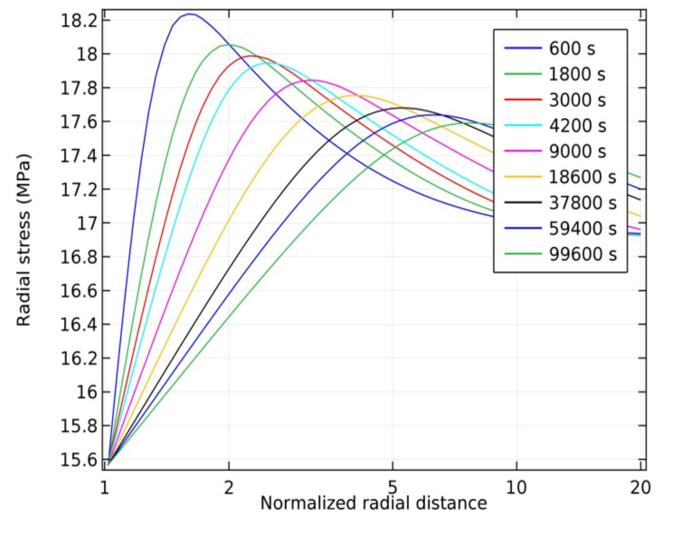
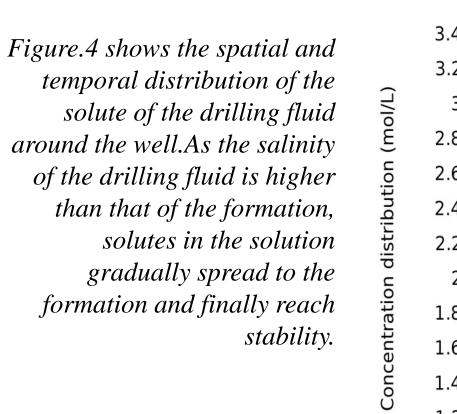
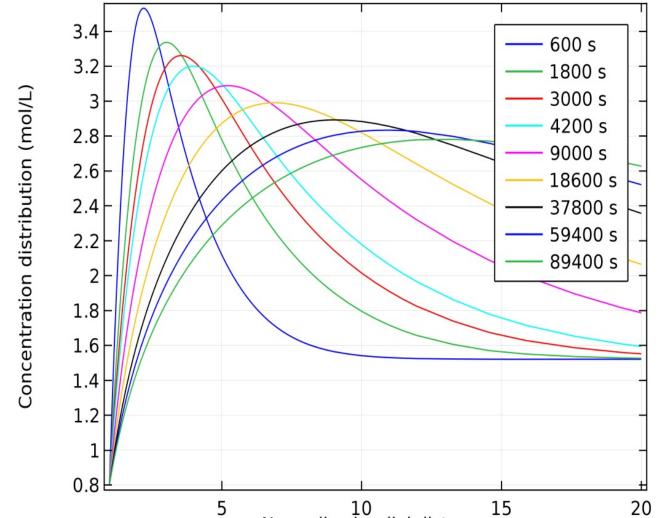


Figure.3 shows the distribution of radial stress around shale gas Wells over time. From the solution results, the stress peak is not in the hole wall out, but in the formation with a certain distance from the hole wall. This is quite consistent with reality. In actual drilling, there are large collapse slabs in the mud returned from the top, which fully shows that the fracture point of mud shale section is at a certain distance from the well wall. This result is consistent with Ghassmi's paper results.





The drilling engineer is very concerned about the stress and chemical physical state around the well. The stress state around the hole can be simulated well by using COMSOL software. This can help engineers solve engineering problems.

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